

## Insight into the Narrow Structure in $\eta$ Photoproduction on the Neutron from Helicity-Dependent Cross Sections

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The double polarization observable  $E$  and the helicity dependent cross sections  $\sigma_{1/2}$  and  $\sigma_{3/2}$  were measured for  $\eta$  photoproduction from quasifree protons and neutrons. The circularly polarized tagged photon beam of the A2 experiment at the Mainz MAMI accelerator was used in combination with a longitudinally polarized deuterated butanol target. The almost  $4\pi$  detector setup of the Crystal Ball and TAPS is ideally suited to detect the recoil nucleons and the decay photons from  $\eta \rightarrow 2\gamma$  and  $\eta \rightarrow 3\pi^0$ . The results show that the narrow structure previously observed in  $\eta$  photoproduction from the neutron is only apparent in  $\sigma_{1/2}$  and hence, most likely related to a spin-1/2 amplitude. Nucleon resonances that contribute to this partial wave in  $\eta$  production are only  $N(1535) 1/2^- (S_{11})$  and  $N(1670) 1/2^+ (P_{11})$ . Furthermore, the extracted Legendre coefficients of the angular distributions for  $\sigma_{1/2}$  are in good agreement with recent reaction model predictions assuming a narrow resonance in the  $P_{11}$  wave as the origin of this structure.

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Photoproduction of  $\eta$  mesons is important for the investigation of the nucleon excitation spectrum. Because of its isoscalar nature, the  $\eta$  only couples to isospin  $I = 1/2$   $N^*$  resonances. In the threshold region,

this reaction is completely dominated by the excitation of the  $N(1535) 1/2^-$  resonance [1] and at higher incident photon energies, contributions from several other excited nucleon states have been identified [2]. Currently, a large

effort is underway at modern photon-beam facilities (see Ref. [2] for a recent summary) to study the  $\gamma p \rightarrow p\eta$  reaction using both single and double polarization observables. However, during the last few years, photoproduction of  $\eta$  mesons off the neutron has attracted additional interest. The reason is the discovery of an unusually narrow structure in the excitation function at incident photon energies of 1 GeV (corresponding to an  $\eta$ -neutron invariant mass of  $W \approx 1.67$  GeV). This structure was first observed by the GRAAL Collaboration [3] and confirmed by the CBELSA/TAPS Collaboration [4,5] in Bonn, and at LNS in Sendai [6]. Recent high-statistics measurements at the MAMI facility in Mainz with deuterium and  $^3\text{He}$  targets [7–9] have extracted a position of the narrow structure of  $W = (1670 \pm 5)$  MeV with a width of only  $\Gamma = (30 \pm 15)$  MeV. This structure is not observed in  $\eta$  photoproduction off the proton [10]. The cross section of  $\gamma p \rightarrow p\eta$  shows only a small dip at this energy [2,10]. However, recently, two narrow structures were observed in the beam asymmetry  $\Sigma$  of Compton scattering of the proton [11]. One of these structures appears close to the above discussed peak in  $\eta$  production off neutrons and the other at  $W \approx 1.726$  GeV. Meanwhile, a counterpart of the latter peak was also unambiguously identified in the cross section of the  $\gamma n \rightarrow n\eta$  reaction [12].

The nature of these structures has not yet been established. The prominent peak observed in  $\eta$  production off the neutron at  $W \approx 1.67$  GeV has been discussed as a new narrow resonance (with exotic properties) [13–17]. It is currently listed in the Review of Particle Physics (RPP) [18] as a tentative  $N(1685)$  state with unknown spin and parity. However, other works suggest coupled-channel effects of known nucleon resonances [19,20], or contributions from intermediate strangeness states [21] as the underlying cause. A fit [22] from the Bonn-Gatchina (BnGa) group to the high statistics MAMI deuteron data [7,9] suggests an interference in the  $J^P = 1/2^-$  partial wave between contributions from the well-known  $N(1535)$  and  $N(1650)$  resonances. Fits of these unpolarized data with the BnGa model including a narrow  $P_{11}$ -like  $N(1685)$  resonance were seen as inferior [22].

The aim of the present work is to determine the relevant partial wave directly from experimental data. For this purpose, the double polarization observable  $E$  was measured with a longitudinally polarized target and a circularly polarized photon beam. It is defined as [23]

$$E = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}}, \quad (1)$$

where  $\sigma_{1/2}$  and  $\sigma_{3/2}$  are the helicity dependent cross sections with antiparallel or parallel photon and nucleon spin, respectively. Nucleon resonances with spin  $J = 1/2$  contribute only to  $\sigma_{1/2}$ , while states with spin  $J \geq 3/2$  can also couple to  $\sigma_{3/2}$ . Hence, structures in the  $S_{11}$  or  $P_{11}$  partial waves appear only in  $\sigma_{1/2}$ , but not in  $\sigma_{3/2}$ . So far, in

$\eta$  production, this observable has only been explored for the reaction with free protons [24], for which it turned out to be very powerful in restricting parameters of reaction model analyses.

The experiments were performed at the Mainz MAMI accelerator [25]. Circularly polarized tagged photons [26] were created via the bremsstrahlung process with longitudinally polarized ( $P_e \sim 80\%$ ) electrons. The beam helicity was flipped once per second. The polarization of the electron beam was measured daily with Mott scattering (after the linac stage of the accelerator at electron energies of 3.65 MeV) and constantly monitored with Møller scattering of the high energy electrons from the bremsstrahlung radiator. The polarization of the photon beam was deduced from the energy-dependent polarization transfer factors given by Olsen and Maximon [27]. The deuterated butanol ( $\text{C}_4\text{D}_9\text{OD}$ ) target was polarized in the longitudinal direction using dynamic nuclear polarization [28]. The target polarization was measured before and after data taking using an NMR measurement technique and was interpolated by an exponential function. Because of small inhomogeneities of the polarizing magnetic field, the target was not homogeneously polarized across its diameter for the initial beam times (so that the NMR measurements did not correctly reflect the polarization degree in the target area interacting with the beam). Therefore, results were renormalized to the final data taking period for which this problem was resolved.

The experimental setup combined the Crystal Ball (CB) [29] and TAPS [30] calorimeters with additional detectors for charged particle identification [31] and covered 98% of  $4\pi$ . The photons from the  $\eta$  decays (results from  $\eta \rightarrow \gamma\gamma$  and  $\eta \rightarrow 3\pi^0 \rightarrow 6\gamma$  were consistent and have been averaged) and the recoil nucleons were detected and analyzed. The detector was identical to the setup used for the measurements with unpolarized targets which is discussed in detail in Refs. [8,9]. Also, all analysis procedures were identical to those described in these references. This includes the clean identification of  $\eta$  production off quasifree nucleons, the Monte Carlo simulations of the detector response, and the reconstruction of final-state kinematics used to remove the effects from nuclear Fermi motion. The latter is essential for the investigation of narrow structures.

The only complication resulted from the contribution from nucleons bound in the unpolarized carbon (and oxygen) nuclei in the butanol target. This background contributes only in the denominator of Eq. (1). It was determined from a measurement with a carbon foam target (which had identical geometry and density to the butanol target) and subtracted. Both measurements (butanol and carbon target) were normalized absolutely to photon fluxes, target surface densities, and detection efficiencies.

The double polarization observable  $E$  for  $\eta$  mesons in coincidence with recoil protons and neutrons is shown in Fig. 1. The systematic uncertainty was estimated from the uncertainty of the target ( $\pm 10\%$ ) and photon beam

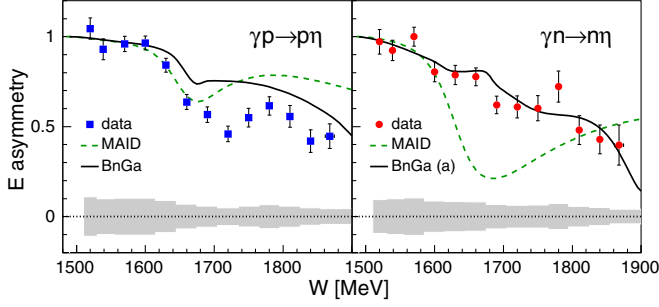


FIG. 1. Double polarization observable  $E$  for  $\gamma p \rightarrow p\eta$  (left-hand side) and  $\gamma n \rightarrow n\eta$  (right-hand side). Gray shaded areas: systematic uncertainties. Curves: predictions from MAID (green, dashed) [32] and BnGa (model based on  $S_{11}$  interference) [22] (black, solid line).

polarization ( $\pm 2.7\%$ ). In addition, there is a small uncertainty related to the subtraction of the carbon background (all other uncertainties, e.g., from detection efficiencies, cancel to a large extent in the ratio of Eq. (1). This uncertainty was estimated from the precision of the photon flux measurements and the determination of the target surface densities. It is on the order of 2.5% and was added quadratically to the polarization degree uncertainties. As a cross check for the correct subtraction of the carbon background an analysis was done for which the

denominator of the ratio in Eq. (1) was replaced by  $2\sigma_0$ , where  $\sigma_0$  is the unpolarized total cross section measured with a liquid deuterium target (so that no subtraction of carbon data is necessary). The data for  $\sigma_0$  were taken from Ref. [9]. The average deviation between the analyses using the carbon subtracted butanol or the liquid deuterium data in the denominator was 2.25% for recoil neutrons and 2.1% for recoil protons. For the latter, only data above  $W = 1.6$  GeV were used for the comparison because for lower energies the detection efficiency for recoil protons [which cancels as long as Eq. (1) is used with the carbon subtracted butanol data] could not be determined precisely enough for a comparison to the results of Ref. [9] on an absolute scale.

The neutron data are in quite good agreement with the results from the BnGa model [22] and clearly rule out the MAID predictions [32]. The disagreement between measurement and MAID prediction can be easily traced to an unrealistically large contribution of the  $N(1675) 5/2^-$  state in the MAID model.

The helicity dependent cross sections  $\sigma_{1/2}$  and  $\sigma_{3/2}$  can be extracted as

$$\sigma_{1/2} = \sigma_0(1 + E), \quad \sigma_{3/2} = \sigma_0(1 - E), \quad (2)$$

from the asymmetry  $E$  and the unpolarized cross section  $\sigma_0$ . For the latter the results from Ref. [9] were used. The results are summarized in Figs. 2 and 3. The systematic

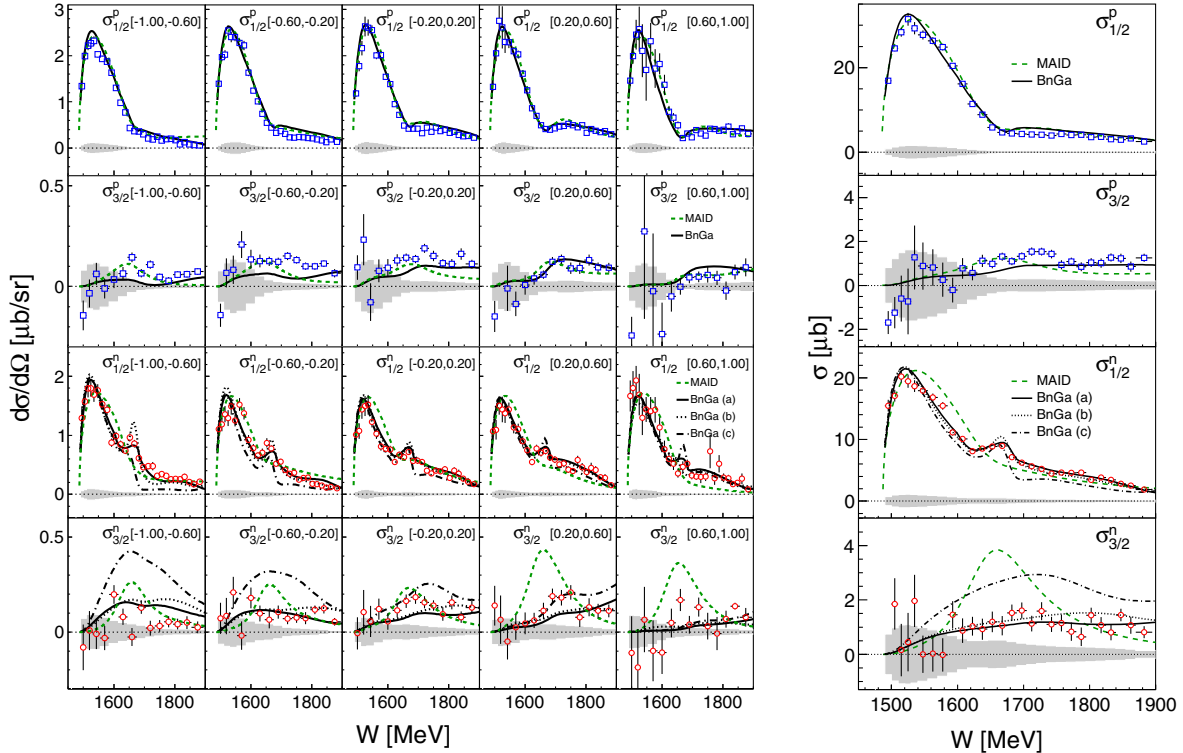


FIG. 2. Excitation functions for  $\sigma_{1/2}$  and  $\sigma_{3/2}$  for five  $\cos(\theta^*)$  bins [ $\cos(\theta)$  ranges given in figure]. Top two rows: results for  $\gamma p \rightarrow p\eta$  (blue squares). Bottom two rows:  $\gamma n \rightarrow n\eta$  (red circles). Gray shaded areas: systematic uncertainties. Curves: model predictions from MAID (dashed green line) [32], BnGa(a) (model version with interference in  $S_{11}$  wave, solid black line) [22], BnGa(b) (model with narrow  $P_{11}$  resonance with positive  $A_{1/2}$  coupling, dotted black line) [22], and BnGa(c) (narrow  $P_{11}$  resonance with negative  $A_{1/2}$  coupling, dash-dotted, black line) [22]. Right hand side: total cross sections.

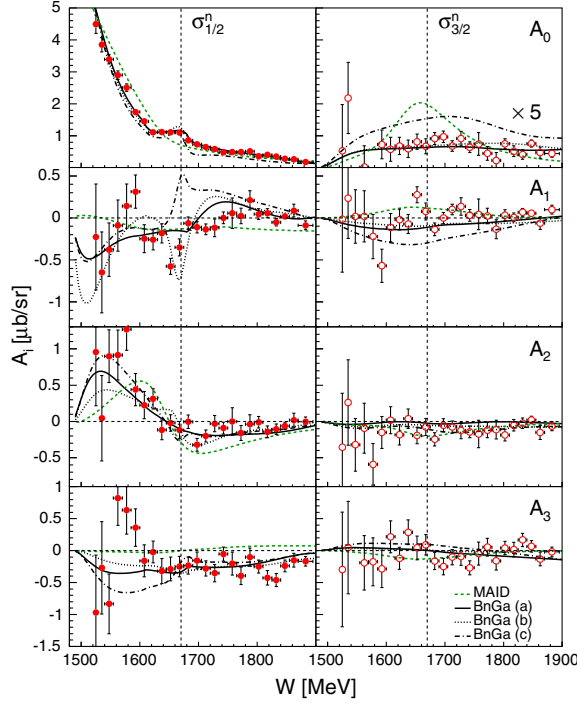


FIG. 3. Legendre coefficients of the angular distributions of  $\sigma_{1/2}$  and  $\sigma_{3/2}$  for the reaction  $\gamma n \rightarrow n\eta$ . Experimental results (red circles) and model predictions by MAID [32] and BnGa [22]. Same notation as in Fig. 2. The vertical dashed lines at  $W = 1685$  MeV indicate the position of the narrow structure. The results for  $A_0$ ,  $\sigma_{3/2}$  are up-scaled by a factor of 5.

uncertainties for  $E$  were propagated into Eq. (2). The overall systematic uncertainty for the scale of  $\sigma_0$  from Ref. [9] is on the order of 7%–15%. It is also possible to construct  $\sigma_{1/2}$  and  $\sigma_{3/2}$  directly from the data measured with the butanol target after subtraction of the carbon background without using input from the independent measurement of the unpolarized cross section. For the measurement with recoil neutrons, excellent agreement was found for all energies and center-of-momentum (c.m.) angles of the  $\eta$ , for recoil protons deviations occurred for  $W < 1.6$  GeV due to the known inaccuracies of the proton detection efficiency.

Figure 2 shows the excitation functions for five bins of  $\cos(\theta_\eta^*)$  [ $\theta_\eta^*$  polar angle in the photon-nucleon c.m. frame] and the total cross sections in comparison to the predictions from the MAID [32] and BnGa [22] models. For protons and neutrons, contributions from the helicity-3/2 amplitude are small, which means that nucleon resonances with  $J \geq 3/2$  contribute little. For the proton target, the  $\sigma_{1/2}$  results are in good agreement with model predictions. The small  $\sigma_{3/2}$  part is in reasonable agreement with model results. Details like the contribution of the  $N(1720) 3/2^+$  state (a small enhancement with respect to the model results may be visible in the total  $\sigma_{3/2}$  cross section in this energy range) will be subject to more refined partial wave analysis.

The results for the quasifree neutron establish that the narrow structure around  $W \approx 1.67$  GeV, listed as the tentative  $N(1685)$  state in RPP, appears only in the helicity-1/2 part of the reaction. This means that it is almost certainly related to  $J = 1/2$  contributions ( $S_{11}$  and/or  $P_{11}$  partial waves). Although excited nucleon states with  $J \geq 3/2$  can also contribute to helicity 1/2, it is unlikely that they contribute *only* to helicity 1/2. The RPP [18] lists only one state up to excitation energies of 2 GeV for which the helicity coupling  $A_{1/2}$  is larger than  $A_{3/2}$  (the  $N(1875) 3/2^+$  for the proton, but even in that case within uncertainties  $A_{3/2}$  could be larger). There is no example for such a state for which the helicity-3/2 contribution is negligible compared to helicity 1/2. Since no trace of the structure is observed in helicity 3/2, a contribution from  $J \geq 3/2$  states is highly unlikely.

As mentioned above, a large contribution of the  $N(1675) 5/2^-$  state, as in the MAID model, was ruled out. In addition, the BnGa model with a narrow  $P_{11}$  resonance with negative coupling disagrees with the experimental results, while the other two BnGa model versions give similar results. The angular distributions have been fitted with third order Legendre expansion to allow for a more detailed comparison to model predictions:

$$\frac{d\sigma}{d\Omega}(W, \cos(\theta_\eta^*)) = \frac{q_\eta^*(W)}{k_\gamma^*(W)} \sum_{i=0}^3 A_i(W) P_i(\cos(\theta_\eta^*)), \quad (3)$$

where  $q_\eta^*$  and  $k_\gamma^*$  are the  $\eta$  and photon momenta in the c.m. frame, respectively. The results are shown in Fig. 3. The  $A_1$  coefficient for the  $\sigma_{1/2}$  cross section is very interesting. An interference between a  $P_{11}$  wave and the dominant  $S_{11}$  wave results in a  $\cos(\theta_\eta^*)$  term in the angular distribution, which is reflected in the  $A_1$  coefficient. Depending on the sign of the interference term, a narrow  $P_{11}$  resonance will result in a sharp positive or negative peak in  $A_1$ , as shown by the model curves in Fig. 3, while interference effects in the  $S_{11}$  wave produce different patterns. The results clearly rule out the model version with a negative  $P_{11} - S_{11}$  interference sign. However, the model results with a positive interference sign of  $P_{11}$  and  $S_{11}$  are more similar to the measured data than the predictions without the addition of a narrow  $P_{11}$  state.

In summary, the double polarization observable  $E$  and the related helicity dependent cross sections  $\sigma_{1/2}$  and  $\sigma_{3/2}$  were measured for the first time for the photoproduction of  $\eta$  mesons on quasifree nucleons using a circularly polarized photon beam and a longitudinally polarized target. The measurement provided data of excellent quality, which are important input for future partial wave analysis of photoproduction of  $\eta$  mesons off nucleons. Here, we report one striking finding about the nature of the narrow structure previously observed in the  $\gamma n \rightarrow n\eta$  reaction. The results have unambiguously established that this structure is related to the helicity-1/2 amplitude and a comparison



of the angular dependence to different model predictions favors a scenario with a contribution from a narrow  $P_{11}$  resonance.

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